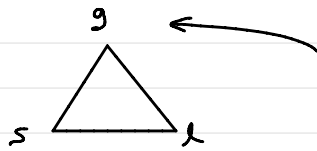


1411 - E3
CH 09 - Gases

9

Chapter 09: Gases



- Comp
- fixed vol
- fixed shape

molecules far apart

Gas Pressure [9.1]

[P 448/456]

↳ atm pressure (1 atm) - pressure at sea level exerted by a column of air 1 m^2 and extending to space.

↳ def:

$$P = F/A$$

$$P = \frac{F}{A} = \frac{1 \text{ Kg} \cdot \text{m}}{\text{s}^2} \bigg| \frac{1}{\text{m}^2} = \frac{1 \text{ Kg}}{\text{s}^2 \text{ m}} = 1 \text{ Pa}$$

F = Newton A in m^2 Pascal

Pressure Units

Unit Name and Abbreviation	Definition or Relation to Other Unit
pascal (Pa)	1 Pa = 1 N/m ² recommended IUPAC unit
kilopascal (kPa)	1 kPa = 1000 Pa
pounds per square inch (psi)	air pressure at sea level is ~14.7 psi
atmosphere (atm)	1 atm = 101,325 Pa air pressure at sea level is ~1 atm
bar (bar, or b)	1 bar = 100,000 Pa (exactly) commonly used in meteorology
millibar (mbar, or mb)	1000 mbar = 1 bar
inches of mercury (in. Hg)	1 in. Hg = 3386 Pa used by aviation industry, also some weather reports
torr	1 torr = $\frac{1}{760}$ atm named after Evangelista Torricelli, inventor of the barometer
millimeters of mercury (mm Hg)	1 mm Hg ~1 torr

Table 9.1

EX: PRESSURE UNIT CONVERSIONS

[EX: 9.15]

2 A typical barometric pressure in Kansas City is 740 torr. What is this pressure in atmospheres, in millimeters of mercury, in kilopascals, and in bar?

$$\textcircled{a} \Delta_{\text{atm}} = \frac{740 \text{ torr}}{760 \text{ torr}} = \boxed{0.97} \times \leftarrow \text{book is wrong...} \right. \\ \left. \dots \text{only 2 s.f.} \right.$$

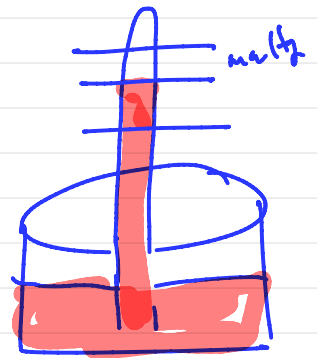
$$\textcircled{b} \Delta_{\text{mm Hg}} = \frac{740 \text{ torr}}{1 \text{ torr}} = \boxed{740} \text{ mm Hg}$$

BAROMETER

Barometer - tube closed at one end, filled w/ NV Liquid, and inverted into bath of the same NV Liquid.

hydrostatic pressure - pressure fluid exerts due to pull of gravity

$$\boxed{P = h\rho g} \quad h = \text{height}; \rho = \text{density}; g = \text{acceleration of gravity}$$



EX: CALC COLUMN HEIGHT VIA PRESSURE [EX 9.26]

Calculate the height of a column of water at 25 °C that corresponds to normal atmospheric pressure. The density of water at this temperature is 1.0 g/cm³.

$P = \rho h g \rightarrow h = \frac{P}{\rho g} = \frac{P}{\rho g}$

$$\frac{1 \text{ atm}}{1} = \frac{1 \text{ atm}}{1.0 \text{ g/cm}^3 \cdot 9.81 \text{ m/s}^2} = \frac{101,325 \text{ Pa}}{1000 \text{ kg/m}^3 \cdot 9.81 \text{ m/s}^2} = 10.3287 \text{ m} = \boxed{10.3 \text{ m}}$$

↑
↑
↑
P
ρ
g

MANOMETER

manometer - gas vessel connected to U-tube containing Non Volatile Liquid (NVL)
- may be open or closed end.

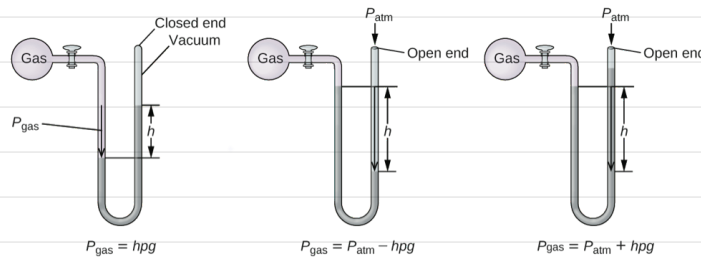


Figure 9.5 A manometer can be used to measure the pressure of a gas. The (difference in) height between the liquid levels (h) is a measure of the pressure. Mercury is usually used because of its large density.

SPHYGMOMANOMETER : MEASURE HUMAN BLOOD PRESSURE

sphygmomanometer (Greek sphygmos = "pulse"). It consists of an inflatable cuff to restrict blood flow, a manometer to measure the pressure, and a method of determining when blood flow begins and when it becomes impeded (Figure 9.6)

Relating Pressure, Volume, Amount, and Temperature:

The Ideal Gas Law [9.2]

[P 457/465]

Early scientist couldn't measure much, but they could:

- TEMPERATURE

- VOLUME

- PRESSURE ← 1644 Torricelli invented the mercury barometer

(also, called empty space above the Hg a "vacuum")

$$P = kT$$

$$P = k \frac{n}{V}$$

Pressure and Temperature: Amontons's Law

/ Gay-Lussac's Law

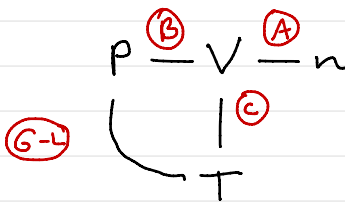
Volume and Temperature: Charles's Law

$$PV = k$$

Volume and Pressure: Boyle's Law

$$\frac{P}{T} = \frac{1}{V}$$

Moles of Gas and Volume: Avogadro's Law



The Ideal Gas Law

[P467/475]

$$\begin{array}{c|c|c|c|c} P & V & = & k & \\ P & & = & k' & T \\ V & & = & k'' & T \\ V & = & n & k''' & \end{array}$$

$$PV = nRT$$

$$\begin{aligned} R &= \frac{0.08206 \text{ atm} \cdot \text{L}}{\text{mol} \cdot \text{K}} \\ &= \frac{8.314 \text{ kPa} \cdot \text{L}}{\text{mol} \cdot \text{K}} = \frac{8.314 \text{ J}}{\text{mol} \cdot \text{K}} \\ &= \frac{1.987 \text{ cal}}{\text{mol} \cdot \text{K}} \end{aligned}$$

* TEMP must be in KELVIN

THREE THINGS YOU NEED TO KNOW TO SOLVE ANY KL Qs:

I

Standard Conditions of Temperature and Pressure

↳ "STP"

↳ $T = 273.15 \text{ K}$ (exact)

↳ $P = 1 \text{ atm}$ (exact) / 101.325 kPa

↳ @ STP, volume of IDEAL GAS =

$$\boxed{\frac{22.4 \text{ L}}{\text{mol}}}$$

(i) @ STP
(ii) ideal gas

II

COMBINED IGL (BEFORE - AFTER SCENARIOS)

changing system

$$\boxed{R = \frac{PV}{nT} = \frac{P'V'}{n'T'}}$$

stationary system

ε A ST
↑

Stoichiometry of Gaseous Substances, Mixtures, and Reactions [9.3]

Density of a Gas

+ OTHER SAMPLE CALCULATIONS

EX: 1 GL - Calc P & density [Wq: 50C 12-45]

$$PV = nRT$$

$$\downarrow$$

$$n = \frac{PV}{RT}$$

- 15.5 (a) A chemist is preparing to carry out a reaction at high pressure that requires 36.0 mol of hydrogen gas. The chemist pumps the hydrogen into a 15.5-L rigid steel container at 25°C. To what pressure (in atmospheres) must the hydrogen be compressed? (b) What would be the density of the high-pressure hydrogen?

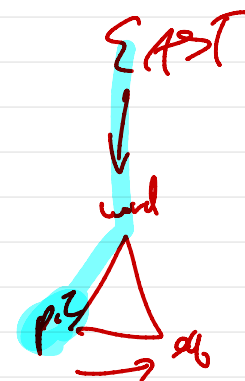
V =	15.5 L
n =	36.0 mol H ₂
T =	298 K
P = ?	56.8 atm

R

$$\frac{1 \text{ atm}}{1} = \frac{0.0821 \text{ atm} \cdot \text{L}}{\text{mol} \cdot \text{K}} \times \frac{36.0 \text{ mol}}{15.5 \text{ L}} \times \frac{298 \text{ K}}{1} = 56.8 \text{ atm}$$

(b) $d = \frac{m}{V} = \frac{\square \text{ g}}{\square \text{ L}} = \frac{36.0 \text{ mol} \times 2.02 \text{ g/mol}}{1 \text{ mol} \times 15.5 \text{ L}} = 4.69 \text{ g/L}$

H₂ is a gas

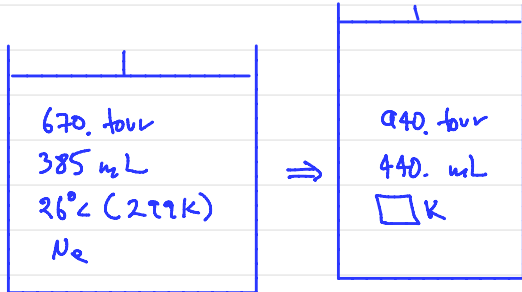


EX: COMBND 16L

[w9: 12-35]

i

A ³⁸⁵280.-mL sample of neon exerts a pressure of ⁶⁷⁰660. torr at 26°C. At what temperature in °C would it exert a pressure of 940. torr in a volume of 440. mL?



$$1 = \frac{\overset{940}{P'} \overset{440}{V'} \overset{299}{T}}{\underset{670}{P} \underset{385}{V} \underset{?}{T'}}$$

↓

$$T' = \boxed{479 \text{ K}}$$

BEFORE → AFTER
(changing (non-static) sys)

$$\frac{\overset{P'}{P} \overset{V'}{V}}{\overset{T}{T}} = \frac{\overset{P'}{P} \overset{V'}{V}}{\overset{T}{T}} \Rightarrow T = \frac{P' V' T}{P V}$$

$$\frac{P' V' T}{P V}$$



Molar Mass of a Gas

ΣAST



Ex: IGL - Calc MW

[W9: 12-56 202]

- c. A cylinder was found in a storeroom of a manufacturing plant. The label on the cylinder was gone and no one remembered what the cylinder held. A 0.00500-gram sample was found to occupy 4.13 mL at 23°C and 745 torr. The sample was also found to be composed of only carbon and hydrogen. Identify the gas.

$$PV = nRT \xrightarrow{n = \frac{g}{MW}} PV = \frac{gRT}{MW}$$

C_xH_y
practice

$$MW = \frac{g}{n}$$
$$\downarrow$$
$$n = \frac{g}{MW}$$

$$\frac{MW}{1} = \frac{gRT}{PV}$$
$$=$$

(Ans next page)

~~ΣAST~~

Molar Mass of a Gas

Ex: 1GL - Calc MW

[W9: 12-56 202]

- c A cylinder was found in a storeroom of a manufacturing plant. The label on the cylinder was gone and no one remembered what the cylinder held. A 0.00500-gram sample was found to occupy 4.13 mL at 23°C and 745 torr. The sample was also found to be composed of only carbon and hydrogen. Identify the gas.

	C_xH_y
(m)	0.00500g
V	4.13 mL
P	745 torr
T	296 K (23°C)

Need MW!!!

$$PV = nRT = \frac{gRT}{MW} \Rightarrow MW = \frac{gRT}{PV}$$

$$MW = \frac{0.00500g}{0.00413L} \times \frac{0.0821 \text{ atm}\cdot\text{L}}{\text{mol}\cdot\text{K}} \times 296K \times \frac{760 \text{ torr}}{745 \text{ torr}} = 30.0 \text{ g/mol}$$

C_1H_{18}
X
 impossible

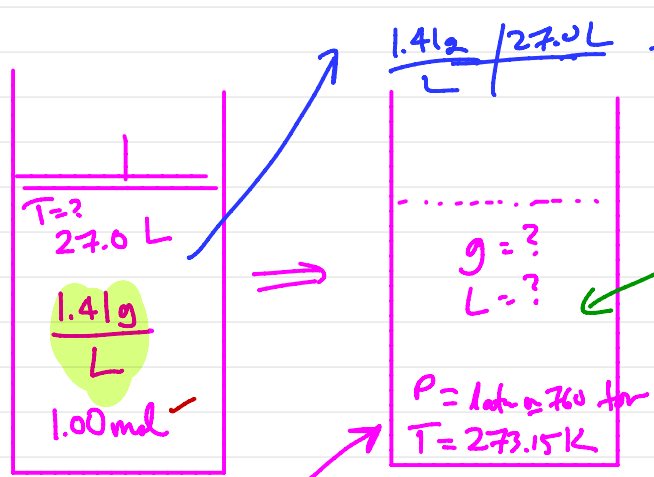
C_2H_6
✓

C_3H_6
X
 impossible

SAST

EX: 1GL - MW & Density & STP

1.00 mol of an unknown gas at an unknown Temp & Pressure, occupies 27.0 Liters and has a density of 1.41 g/L. @ What is its Density at STP @ What is its MW?



$PV = nRT$
 $V = \frac{nRT}{P}$

Know
 ↓
 calc
 ↓
 look up

$V = \frac{nRT}{P} = \frac{1.00 \text{ mol} \cdot 0.0821 \text{ L} \cdot \text{atm} / \text{mol} \cdot \text{K} \cdot 273.15 \text{ K}}{1 \text{ atm}}$

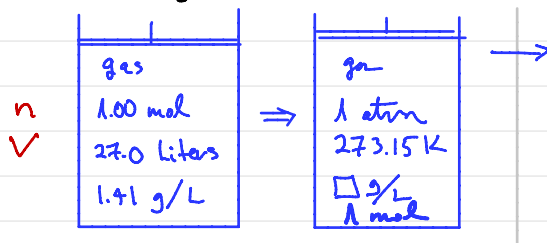
$\frac{\square \text{ g}}{\square \text{ L}} = \frac{38.1 \text{ g}}{22.4 \text{ L}} = 1.70 \text{ g/L} = 22.4 \text{ L}$

$MW = \frac{\square \text{ g}}{\square \text{ mol}} = 38.1 = MW$

(ANS next page)

EX: IGL - MW & Density & STP

i 1.00 mol of an unknown gas, at an unknown Temp & Pressure, occupies 27.0 Liters and has a density of 1.41 g/L. @ What is its Density at STP. @ What is its MW?



$$d = \frac{\square \text{ g}}{\square \text{ L}} = \frac{38.1 \text{ g}}{22.4 \text{ L}} = 1.70 \text{ g/L}$$

Ⓐ $\square \text{ g} = \frac{1.41 \text{ g}}{\text{L}} \times 27.0 \text{ L} = 38.1 \text{ g}$

Ⓙ $\text{MW} = \frac{\square \text{ g}}{\square \text{ mol}} = \frac{38.1 \text{ g}}{1.00 \text{ mol}} = 38.1 \text{ g/mol}$

Ⓚ $V = \frac{nRT}{P} = \frac{1.00 \text{ mol} \times 0.0821 \text{ atm}\cdot\text{L}}{\text{mol}\cdot\text{K}} \times \frac{273.15 \text{ K}}{\text{atm}} = 22.4 \text{ L}$

EX: 16L - static sys, calc vol [49: 5x12-9, int+xt]

What is the volume of a gas balloon filled with 4.00 moles of He when the atmospheric pressure is 748 torr and the temperature is 30.°C?

$$\frac{\square L}{1} = \frac{4.00 \text{ mol} \mid 0.0821 \text{ atm} \cdot \text{L}}{\text{mol} \cdot \text{K}} \mid \frac{303.15 \text{ K}}{0.984 \text{ atm}}$$

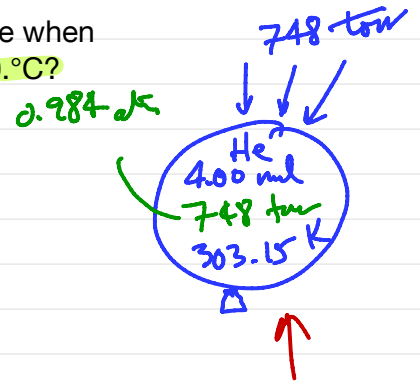
$$= \boxed{101 \text{ L}}$$

$$PV = nRT \quad \leftarrow \text{STATIC}$$

$$V = \frac{nRT}{P}$$

$$\frac{\square L}{1} = \frac{0.0821 \text{ atm} \cdot \text{L}}{\text{mol} \cdot \text{K}} \mid \frac{4.00 \text{ mol} \mid 303.15 \text{ K}}{0.984 \text{ atm}}$$

(ANS next page)



EX: 16L - STATED SYD, CALC VOL [W9: 5X12-9, INT+XT]

¿ What is the volume of a gas balloon filled with 4.00 moles of He when the atmospheric pressure is 748 torr and the temperature is 30.°C?

He
4.00 mol
748 torr (0.984 atm)
30.°C (303 K)

$$\square V = \frac{nRT}{P} = \frac{4.00 \text{ mol} \times 0.0821 \text{ atm} \cdot \text{L} / \text{mol} \cdot \text{K} \times 303 \text{ K}}{0.984 \text{ atm}} = \square 101 \text{ L}$$

↑
If "stated" problem,
go ahead and make
conv. to match "R"

EX: IGL - STATIC SYS - Calc "g" [W9: 12-10, in feet]

Ĉ A helium-filled weather balloon has a volume of 7240 cubic feet. How many grams of helium would be required to inflate this balloon to a pressure of 745 torr at 21°C? (1 ft³ = 28.3 L)

practice

(Ans ↓)

EX: IGL - STATIC Sys - Calc "g" [W9: 12-10, in feet]

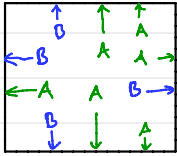
Ĉ A helium-filled weather balloon has a volume of 7240 cubic feet. How many grams of helium would be required to inflate this balloon to a pressure of 745 torr at 21°C? (1 ft³ = 28.3 L)

He
7240 ft ³
745 torr (0.980 atm)
21°C (294 K)

$$PV = nRT = \frac{g}{MW} RT \Rightarrow g = \frac{P V MW}{RT}$$

$$\square g = \frac{0.980 \text{ atm} \times \text{mol} \cdot \text{K} \times 7240 \text{ ft}^3 \times 28.3 \text{ L}}{294 \text{ K} \times 0.0821 \text{ atm} \cdot \text{L} \times (\text{ft}^3) \times \text{mol}} = \boxed{33,300 \text{ g}}$$

The Pressure of a Mixture of Gases: Dalton's Law



$$P_T = \sum P_i = P_a + P_b + P_c \dots$$

PARTIAL PRESSURE: pressure exerted by each individual gas

Mole Fraction (X): $\left(\frac{\text{part}}{\text{whole}} \times 100\right)$ where part, whole expressed in moles

$$X_i = \frac{n_i}{n_{\text{TOTAL}}} = \frac{P_i}{P_T}$$

$$P_i V_i = n_i R T_i$$

$$n_i = \frac{P_i V_i}{R T_i}$$

$$X_i = \frac{P_i V_i}{R T_i} \bigg/ \frac{P_T V_T}{R T_T}$$

for gas mixture

$$P_T V_T = n_T R T_T$$

$$\left\{ \begin{array}{l} P_T V_T = n_T R T \\ P_i V_i = n_i R T \end{array} \right.$$

EX: IGL + DALTON - CALC P AND P_i [L9: EX 12-15]

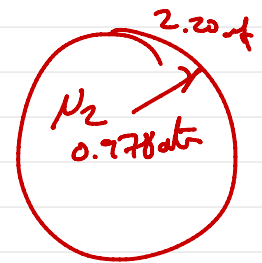
2 A 10.0-liter flask contains 0.200 mole of methane, 0.300 mole of hydrogen, and 0.400 mole of nitrogen at 25°C. (a) What is the pressure, in atmospheres, inside the flask? (b) What is the partial pressure of N₂?

FAST

0.200 mol CH ₄
0.300 " H ₂
0.400 " N ₂
298 K
10.0 L

(a) $PV = nRT \Rightarrow P = \frac{nRT}{V}$

$$P = \frac{(0.200 + 0.300 + 0.400 \text{ mol})}{10.0 \text{ L}} \times \frac{0.0821 \text{ atm} \cdot \text{L}}{\text{mol} \cdot \text{K}} \times 298 \text{ K} = 2.20 \text{ atm}$$



(b) $\frac{n_N}{n_T} = X_N = \frac{P_N}{P_T} \Rightarrow P_N = X_N P_T = \frac{0.400}{0.900} \times 2.20 \text{ atm} = 0.978 \text{ atm}$

= OR =

$$P_N V_N = n_N RT \Rightarrow P_N = \frac{n_N RT}{V_N} = \frac{0.400 \text{ mol} \times 0.0821 \text{ atm} \cdot \text{L}}{\text{mol} \cdot \text{K}} \times \frac{298 \text{ K}}{10.0 \text{ L}} = 0.979 \text{ atm}$$

Collection of Gases over Water

↳ Problem: collected gas is contaminated with water vapor

$$P_T = \sum P_i = P_{\text{gas}} + P_{\text{water}}$$

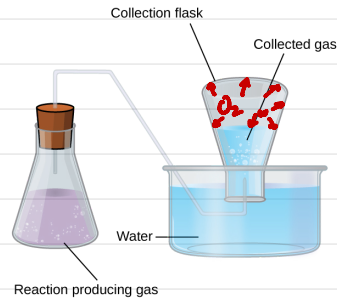
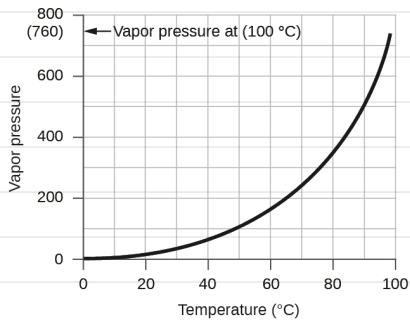
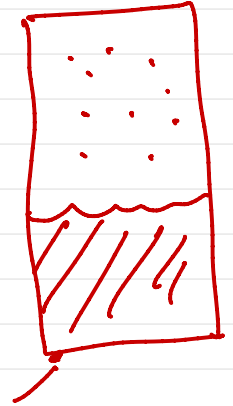


FIG. 9.21

FIG. 9.22



$$P_T = P_{O_2} + P_w$$
$$(P_T - P_w) = P_{O_2}$$

IGL — COLLECTED OVER WATER

[w9.ex12-19, in text]

(EX) Hydrogen was collected over water (Figure 12-7) at 21°C on a day when the atmospheric pressure was 748 torr. The volume of the gas sample collected was 300. mL. <(a) How many moles of H₂ were present? (b) How many moles of water vapor were present in the moist gas mixture? (c) What is the mole fraction of hydrogen in the moist gas mixture?> What would be the mass of the gas sample if it were dry?

$P_H V_H = n_H RT = \frac{g_{H_2} RT}{MW_{H_2}}$

Wet
 T 21°C (294K)
 P 748 torr (0.984 atm)
 V 300. mL (0.300L)
 □ g, H

$P_T = P_{H_2} + P_w$
 $P_{H_2} = P_T - P_w$
 $= 748 \text{ torr} - 18.7 \text{ torr}$
 $= 729 \text{ torr} = 0.960 \text{ atm}$

$g_{H_2} = \frac{P_{H_2} V_{H_2} MW_{H_2}}{R T}$

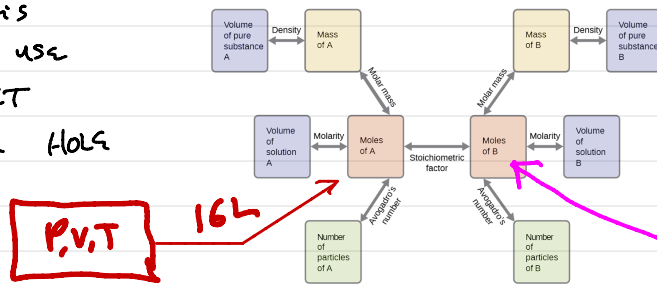
$g_{H_2} = \frac{0.960 \text{ atm} \times 0.300 \text{ L} \times 2.02 \text{ g/mol}}{294 \text{ K} \times 0.0821 \text{ atm} \cdot \text{L/mol} \cdot \text{K}} = 0.0241 \text{ g, H}_2$

Thurs, Nov 21

Chemical Stoichiometry and Gases

[P478/486]

↳ Translation of this section: CAN use $PV=nRT$ TO GET INTO THE MOLE HOLD



Avogadro's Law Revisited

[P478/486]

↳ Punchline: moles gas of volume
 ↳ for Ideal Gas: 22.4 L/mol

$$\frac{14.22 \text{ L}}{22.4 \text{ L/mol}}$$

$$PV = nRT$$

↳

$$n = \frac{PV}{RT}$$

(EX) STOICHIOMETRY OF A GAS USING VOLUME. [ex9.17b]

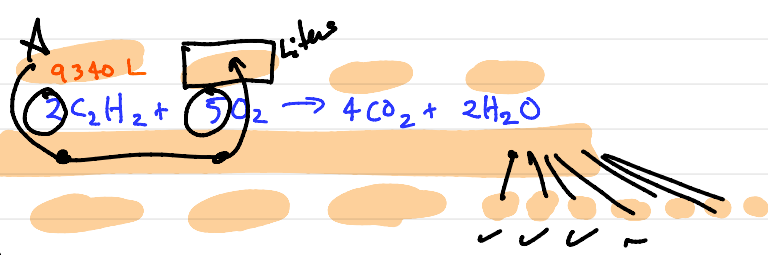
An acetylene tank for an oxyacetylene welding torch provides 9340 L of acetylene gas, C_2H_2 , at $0^\circ C$ and 1 atm. How many tanks of oxygen, each providing $7.00 \times 10^3 L$ of O_2 at $0^\circ C$ and 1 atm, will be required to burn the acetylene?



"CF simple ratio"

STP = $\left(\frac{22.4L}{mol}\right)$

$\left(\frac{9340L}{\text{tank, Ac}}\right)$
 $\left(\frac{7.00 \times 10^3 L}{\text{tank } O_2}\right)$



C_2H_2
 $273 K$
 $1 atm$

\star
 $\square \text{ tank } O_2 = \frac{9340L \text{ Ac}}{1} \times \frac{5L O_2}{2L \text{ Ac}} \times \frac{1 \text{ Tank } O_2}{7.00 \times 10^3 L O_2} = 3.34 \text{ tanks } O_2$

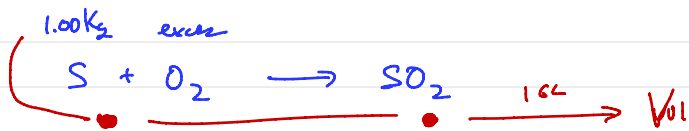
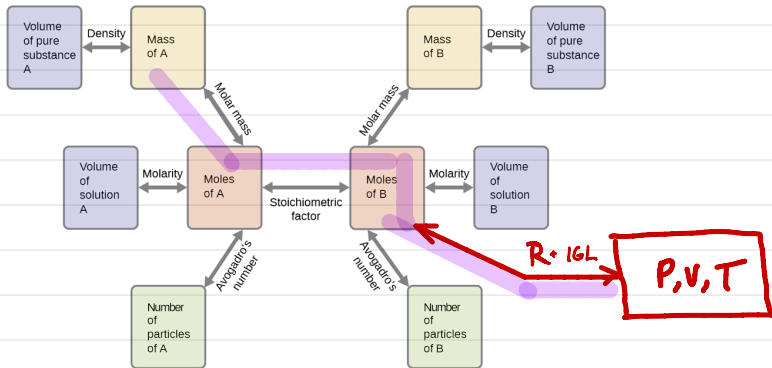
$\frac{9340L}{22.4L/mol} \times \frac{1 mol \text{ Ac}}{2 mol \text{ Ac}} \times \frac{5 mol O_2}{1 mol O_2} \times \frac{1 \text{ Tank } O_2}{7.00 \times 10^3 L O_2} \dots$

CAUTION # 1: ASSUMES IDEAL GASES
CAUTION # 2: ALL GASES AT SAME TEMP & PRESSURE

$\dots \frac{1 \text{ Tank } O_2}{7.00 \times 10^3 L O_2}$

EX: STOICHIOMETRY OF GASES: mol_A → vol_B [ex 9.196]

¿Sulfur dioxide is an intermediate in the preparation of sulfuric acid. What volume of SO₂ at 343 °C and 1.21 atm is produced by burning 1.00 kg of sulfur in oxygen?



$$\boxed{g, S_2} = \frac{1.00 \text{ kg } S}{1 \text{ kg, } S} \times \frac{1000 \text{ g, } S}{1 \text{ kg, } S} \times \frac{\text{mol, } S}{32.1 \text{ g } S} \times \frac{1 \text{ mol } SO_2}{1 \text{ mol, } S} \times \frac{0.0721 \text{ atm} \cdot \text{L}}{\text{mol} \cdot \text{K}} \times \frac{(343 + 273) \text{ K}}{1.21 \text{ atm}} = 1.30 \times 10^2 \text{ L}$$

use "R" as 1st factor

Effusion and Diffusion of Gases [9.4]

mean free path - avg. distance between collisions

diffusion - dispersal of molecules in space due to differences in concentration

$$\text{rate of diffusion} = \frac{\text{amt of gas passing through an area}}{\text{unit of time}}$$

effusion - escape of gas into lower pressure area through a pinhole

Graham's Law of Effusion

↳ heavier the molecule, the slower it moves

$$\text{rate of effusion} \propto \frac{1}{\sqrt{M}}$$

$$\frac{\text{rate of effusion of A}}{\text{rate of effusion of B}} = \frac{\sqrt{M_B}}{\sqrt{M_A}}$$

Ex: Calc MW from Graham [Collins Outlines, Ex 6.26, P 132]

i An unknown gas effuses at a rate of 0.632 times that of O_2 .
What is the MW of the unknown gas?

$$\frac{\text{rate } O_2}{\text{rate unk}} = \frac{\sqrt{MW_{unk}}}{\sqrt{MW_{O_2}}} \Rightarrow \frac{1}{0.632} = \frac{\sqrt{x}}{\sqrt{32.0}} \Rightarrow x = \left(\frac{\sqrt{32}}{0.632} \right)^2 = \boxed{80.1 \text{ g/mol}}$$

(EX) CALC EFFUSION TIME [ex9.21b]

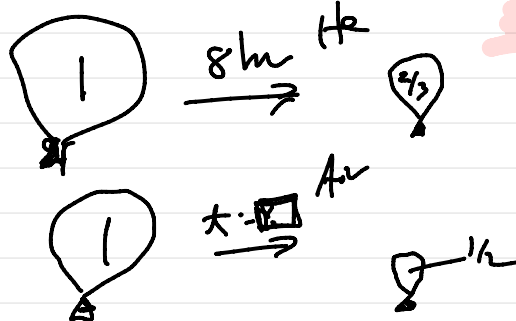
¿A party balloon filled with helium deflates to $\frac{2}{3}$ of its original volume in 8.0 hours. How long will it take an identical balloon filled with the same number of moles of air ($M = 28.2$ g/mol) to deflate to $\frac{1}{2}$ of its original volume?

$\frac{\text{rate}}{\text{rate}'} = \frac{\sqrt{M'}}{\sqrt{M}}$

$\frac{1}{3.8} = \frac{\sqrt{28.2}}{\sqrt{4.0}}$ $\Rightarrow \frac{1}{3.8} = 2.66$

$x = 31.86 = \boxed{32 \text{ hr}}$ $\leftarrow \frac{2x}{24} = 2.66$

$\frac{\text{Vol}}{\text{time}}$



words
pic \rightarrow eq

The Kinetic-Molecular Theory [9.5]

[P488/496]

Kinetic molecular theory (KMT) - simple model to explain gas law obs.

introduce
$$\frac{PV}{nT} = R$$

BASIC TENETS

- ① STRAIGHT-LINE motion, except when hit wall or another
- ② DISCRETE, SMALL PARTICLES, far, far apart $\leftarrow \therefore$ no interaction of influence of other molecules.
- ③ PRESSURE = particles hitting container wall
- ④ PARTICLES ARE UN-INFLUENCED, feel no attraction/repulsion w/ others \leftarrow
- ⑤ $\overline{KE} \propto$ TEMP (in K)

2 Factors

- ① Collision Frequency (often) $\leftarrow n$
- ② Collision Vigor (hard) $\leftarrow T$

Kinetic-Molecular Theory Explains the Behavior of Gases, Part I

molecular Velocities and Kinetic Energy

Kinetic-Molecular Theory Explains the Behavior of Gases, Part II

Non-Ideal Gas Behavior [9.6]

Root Mean Square Velocity

KE of a particle of mass (m) and speed (u) =

$$\textcircled{1} \quad KE = \frac{1}{2} m u^2$$

$$u_{rms} = \sqrt{\bar{u}^2} = \sqrt{\frac{u_1^2 + u_2^2 + u_3^2 \dots}{n}}$$

plug in

$$\textcircled{1} \quad KE_{avg} = \frac{1}{2} m u_{rms}^2$$

charn

$$\textcircled{2} \quad KE_{avg} = \frac{3}{2} RT$$

$$\frac{1}{2} m u_{rms}^2 = \frac{3}{2} RT$$

$$\textcircled{3} \quad u_{rms} = \sqrt{\frac{3RT}{m}}$$

ENERGY vs. SPEED

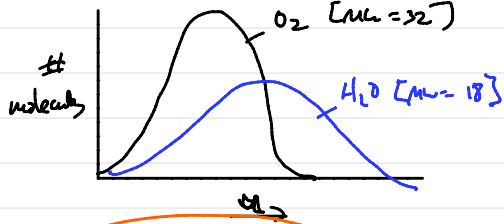
(a) $KE = \frac{1}{2} m u^2$
 (mass points to m , speed points to u)

(b) $T \propto KE = \frac{1}{2} m u^2$
 (MW points to u)

(4) $u \propto \sqrt{\frac{T}{MW}}$

Speed

[MW vs. speed]



[T vs speed]



O₂ @ 25°C, $\bar{u} = \frac{400m}{s} = 895 \text{ mph}$

O₂ @ 1000°C, $\bar{u} = \frac{1600m}{s} = 3,580 \text{ mph}$

Effusion Rate vs. Mass

(derivation of GRAHAM'S LAW)

$$\frac{\text{effusion rate A}}{\text{effusion rate B}} = \frac{u_{\text{rms A}}}{u_{\text{rms B}}} = \frac{\sqrt{\frac{3RT}{m_a}}}{\sqrt{\frac{3RT}{m_b}}} = \sqrt{\frac{m_b}{m_a}} \quad (5)$$

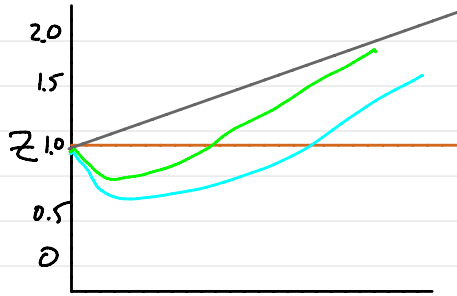
↑
Graham's Law

- rate (u, "rate")
- Temp
- KE
- m/M^2

NON-IDEAL GASES ("REAL WORLD")

$$PV = nRT$$
$$Z = n = \frac{PV}{RT}$$

BECAUSE !!!
High Pressure
Low Temp



$$PV = nRT$$

$$\left(P + \frac{an^2}{V^2} \right) (V - nb) = nRT$$

↑
corrects for
molar attractive

↑
corrects for
volume of
molecule

"a" & "b" are constants.